

# **TCC COURSE ON OUTER SPACE AND AUTOMORPHISMS OF FREE GROUPS**

## **EXERCISES 3**

- (1) The first definition of Outer space  $CV_n$  we gave was in terms of actions on trees. Show that inner automorphisms act trivially on this space, according to the definition we gave of the action.
- (2) Show that if a free simplicial action of  $F_n$  on a tree is minimal, then the quotient graph is finite and has no univalent vertices.
- (3) Show that the dimension of  $CV_n$  is  $3n - 4$ . [Use the Euler characteristic]