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**Conic reduction of graphs for the stable set problem. (English summary)**

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The problem of finding a maximum stable (= independent) set of nodes in a graph has been tackled in various ways. One approach consists in using reduction methods, i.e., trying to associate to a given graph  $G$  with (unknown) stability number  $\alpha(G) = \max\{|S|: S \text{ a stable set in } G\}$  a graph  $G^1$  with  $\alpha(G^1) = \alpha(G) - p$  where  $p$  is a known positive integer (usually  $p = 1$ ). Repeated application of the reduction produces a clique and  $\alpha(G)$  can be easily obtained.

Lozin introduces a conic reduction which does not increase the number of nodes in the graph and which can be performed in polynomial time. This technique allows a computation of  $\alpha(G)$  in polynomial time for a subclass of the graphs  $G$  containing no chair (a chair is a claw with two branches of length one and one branch of length two).

An algorithm in  $O(n^4)$  time is then given for finding  $\alpha(G)$  for a subclass of chair-free graphs characterized by 3 additional forbidden subgraphs (called butterfly, parachute and kite).

Reviewed by *D. de Werra*

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*Note: This list reflects references listed in the original paper as accurately as possible with no attempt to correct errors.*