# MATH 111 HOMEWORK 7, WINTER 2004 

DUE FRIDAY, MARCH 12

(1) Write an algorithm to intersect two monomial ideals $I$ and $J$. You should prove that your algorithm works, and give an example.
(2) State and prove criteria for when $I J=I+J$, where $I$ and $J$ are monomial ideals.
(3) Show that a monomial ideal is prime if and only if it is generated by a subset of the variables.
(4) Recall that a monomial ideal $I$ is radical if and only if it has a squarefree generating set. Give an algorithm to compute monomial prime ideals $P_{1}, \ldots, P_{s}$ such that $I=\cap_{i=1}^{s} P_{i}$. You should prove that your algorithm works, and illustrate it on the ideal $I=\left\langle x_{1} x_{5}, x_{1} x_{3}, x_{3} x_{4}\right\rangle$. Does your algorithm require $k$ to be algebraically closed?

